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Mathematics : Probability Theory and Stochastic Processes

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# Introduction to Stochastic Integration

- Provides a concise introduction to the theory of stochastic integration, also called the Ito calculus
- Closes the gap between more technically advanced books like Karatzas and Shreve (Springer) and less rigorous but more intuitive approaches such as that of Thomas Mikosch (World Scientific)
- Each chapter includes a variety of exercises designed to help the reader further understand the material
- Contains an unusually diverse selection of examples, and an attractive selection of topics

In the Leibniz–Newton calculus, one learns the differentiation and integration of deterministic functions. A basic theorem in differentiation is the chain rule, which gives the derivative of a composite of two differentiable functions. The chain rule, when written in an indefinite integral form, yields the method of substitution. In advanced calculus, the Riemann–Stieltjes integral is defined through the same procedure of “partition-evaluation-summation-limit” as in the Riemann integral. In dealing with random functions such as functions of a Brownian motion, the chain rule for the Leibniz–Newton calculus breaks down. A Brownian motion moves so rapidly and irregularly that almost all of its sample paths are nowhere differentiable. Thus we cannot differentiate functions of a Brownian motion in the same way as in the Leibniz–Newton calculus. In 1944 Kiyosi Itô published the celebrated paper “Stochastic Integral” in the Proceedings of the Imperial Academy (Tokyo). It was the beginning of the Itô calculus, the counterpart of the Leibniz–Newton calculus for random functions. In this six-page paper, Itô introduced the stochastic integral and a formula, known since then as Itô’s formula. The Itô formula is the chain rule for the Itô calculus. But it cannot be expressed as in the Leibniz–Newton calculus in terms of derivatives, since a Brownian motion path is nowhere differentiable. The Itô formula can be interpreted only in the integral form. Moreover, there is an additional term in the formula, called the Itô correction term, resulting from the nonzero quadratic variation of a Brownian motion.

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