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**CD-ROM**

A CD-ROM accompanies this book containing programs for waves in piles, propagation of earthquakes in soils, waves in a half space generated by a line load, a point load, a strip load, or a moving load, and the propagation of a shock wave in a saturated elastic porous material.



<http://www.springer.com/978-90-481-3440-3>

An Introduction to Soil Dynamics

Verruijt, A.

2010, XIV, 433 p. With CD-ROM., Hardcover

ISBN: 978-90-481-3440-3