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Structural Vibration
A Uniform Accurate Solution for Laminated Beams, Plates and Shells with General Boundary Conditions
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