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## PART III. Software Reliability

### Software Reliability Models: A Selective Survey and New Directions

**Siddhartha R. Dalal**

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### Software Reliability Modeling

**James Ledoux**

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