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10 Special Classes of Processes
11 Convergence Concepts and Limit Theorems
12 Ergodic Theory and Stationary Processes
13 Palm Theory
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15 Spatial Point Processes
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