This book, like many other books, was delivered under tremendous inspiration and encouragement from my teachers, research collaborators, and students. My interest in longitudinal data analysis began with a short course taught jointly by K.Y. Liang and S.L. Zeger at the Statistical Society of Canada Conference in Acadia University, Nova Scotia, in the spring of 1993. At that time, I was a first-year PhD student in the Department of Statistics at the University of British Columbia, and was eagerly seeking potential topics for my PhD dissertation. It was my curiosity (driven largely by my terrible confusion) with the generalized estimating equations (GEEs) introduced in the short course that attracted me to the field of correlated data analysis. I hope that my experience in learning about it has enabled me to make this book an enjoyable intellectual journey for new researchers entering the field. Thus, the book aims at graduate students and methodology researchers in statistics or biostatistics who are interested in learning the theory and methods of correlated data analysis.

I have attempted to give a systematic account of regression models and their applications to the modeling and analysis of correlated data. Longitudinal data, as an important type of correlated data, has been used as a main venue for motivation, methodological development, and illustration throughout the book. Given the many applied books on longitudinal data analysis already available, this book is inclined more towards technical details regarding the underlying theory and methodology used in software-based applications. I hope the book will serve as a useful reference for those who want theoretical explanations to puzzles arising from data analyses or deeper understanding of underlying theory related to analyses. This book has evolved from lecture notes on longitudinal data analysis, and may be considered suitable as a textbook for a graduate course on correlated data analysis.

This book emphasizes some recent developments in correlated data analysis.

First, it takes the perspective of Jørgensen’s theory of dispersion models for the discussion of generalized linear models (GLMs) in Chapter 2. It
is known that the class of generalized linear models plays a central role in
the regression analysis of nonnormal data. In the context of correlated data
analysis, these models constitute marginal components in a joint model formulation. One benefit from such a treatment is that it enables this book to cover
a broader range of data types than the traditional GLMs. Two types that are
of particular interest and discussed in detail in the book are compositional (or
continuous proportional) data and directional (or circular) data.

Second, it gives a systematic treatment for the theory of inference functions
(or estimating functions) in Chapter 3. The popular GEE methods presented
in Chapter 5 are then easily introduced and studied as a special class of
inference functions. Building upon Chapter 3, some alternative estimating
function methods can be readily discussed. Recent work on quadratic inference
functions (QIF) is an example that benefits from Chapter 3.

Third, it presents a joint modeling approach to regression analysis of cor-
related data via the technique of parametric copulas. Copulas are becoming
increasingly popular in the analysis of correlated data, and Chapter 6 focuses
on Gaussian copulas, for which both theory and numerical examples are illus-
trated.

Fourth, it deals with state space models for longitudinal data from long
time series. In contrast to longitudinal data from short time series, modeling
stochastic patterns or transitional behaviors becomes a primary task. In such
a setting, asymptotics may be established by letting the length of the time
series tend to \( \infty \), as opposed to letting the number of subjects tend to \( \infty \), as
in the case of data consisting of many short time series. Chapters 10, 11, and
12 are devoted to this topic.

Fifth, this book covers two kinds of statistical inferences in generalized lin-
ear mixed effects models (GLMMs): maximum likelihood inference in Chapter
7 and Bayesian inference based on Markov Chain Monte Carlo (MCMC) in
Chapter 8. In Chapter 8, the analysis of multi-level data is also discussed in
the framework of hierarchical models. Inference can be dealt with easily by the
MCMC method, as an extension from the GLMMs with little extra technical
difficulty.

The book contains some other topics that are highly relevant to the anal-
ysis of correlated data. For example, Chapter 13 concerns missing data prob-
lems arising particularly from longitudinal data.

The presentation of some material in the book is a little technical in order
to achieve rigor of exposition. Readers’ backgrounds should include mathe-
matical statistics, generalized linear models, and some knowledge of statisti-
cal computing, such as represented R and SAS software. The following chart
displays the relationship among the thirteen chapters, and readers can follow
a particular path to reach a topic of interest.
A webpage has been created to provide some supplementary material for the book. The URL address is

http://www.stats.uwaterloo.ca/~song/BOOKLDA.html

All data sets used in the book are available. A SAS Macro QIF is available for a secured download; that is, an interested user needs to submit an online request for permission in order to download this software package. In addition, some figures that are printed in reduced size in the book are supplied in their full sizes. Exercise problems for some of the thirteen chapters are posted, which may be useful when the book is used as a text for a course.

I would like to acknowledge my debt to many people who have helped me to prepare the book. I was fortunate to begin my research in this field under the supervision of Bent Jørgensen, who taught me his beautiful theory of dispersion models. At UBC, I learned the theory of copulas from Harry Joe. This book has benefited from some of the PhD theses that I supervised in the past ten years or so, including Zhenguo (Winston) Qiu, Dingan Feng, Baifang Xing, and Peng Zhang, as well as from a few data analysis projects that graduate students did in my longitudinal data analysis course; thanks go to Eric Bingshu Chen, Wenyu Jiang, David Tolusso, and Wanhua Su. Many graduate students in my course pointed out errors in an early draft of the book. Qian Zhou helped me to draw some figures in the book, and Zichang Jiang worked with me to develop SAS MACRO QIF, which is a software package to fit marginal models for correlated data.

I am very grateful to my research collaborators for their constant inspiration and valuable discussions on almost every topic presented in the book. My great appreciation goes to Annie Qu, Jack Kalbfleisch, Ming Tan, Claudia Czado, Søren Lundbye-Christensen, Jianguo (Tony) Sun, and Mingyao Li. I would also like to express my sincere gratitude to people who generously provided and allowed me to analyze their datasets in the book, including John
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I take full responsibility for all errors and omissions in the book. Finally, I would like to say that given the vast amount of published material in the field of correlated data analysis, the criterion that I adopted for the selection of topics for the book was really my own familiarity. Because of this and space limitations, some worthwhile topics have no doubt been excluded. Research in this field remains very active with many new developments. I would be grateful to readers for their critical comments and suggestions for improvement, as well as corrections.

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